Pre-Calculus 11 Final Review (calculators, formula sheet, scap and graph paper permitted)

Multiple Choice

Identify the choice that best completes the statement or answers the question.

1. Classify the number $\sqrt{\frac{16}{4}}$. I. Positive integer II. Rational number III. Irrational number IV. Real number a. I, II, and IV b. III and IV c. II and IV d. I and II 2. Which set of numbers contains all rational numbers? c. $5, \frac{5}{10}, \sqrt{7}$ a. −5, √10, 0.858585... b. 0, $\sqrt{25}$, $-1.\overline{6}$ d. $-\sqrt{5}$, $-\sqrt{49}$, -3.35d. $\sqrt{3}$ c. 1 5. Which power is equivalent to $(\sqrt[7]{-125})^4$? a. $\frac{4}{7}$ b. $(-125)^{\frac{7}{4}}$ c. $(-125)^{\frac{4}{7}}$ d. $-125^{\frac{7}{4}}$ 6. Which expression is equivalent to $\left(\frac{50}{32}\right)^{-\frac{2}{2}}$? a. $\left(\frac{25}{16}\right)^{\frac{3}{2}}$ b. $\left(\frac{16}{25}\right)^{\frac{2}{3}}$ c. $\sqrt{\left(\frac{16}{25}\right)^{3}}$ d. $\sqrt{\left(\frac{16}{25}\right)^2}$ ____ 7. Write $\frac{1}{25}$ as a power with a negative exponent. c. $(-5)^2$ a. 2⁻⁵ b. 5⁻² d. -5^{-2} 8. Simplify $4x^{-6} \cdot 2x^3$. Write the expression with positive exponents. a. $\frac{x^3}{64}$ b. $\frac{8}{x^3}$ c. $\frac{64}{x^3}$ d. $-\frac{x^3}{8}$

 9.	Evaluate $\left(\frac{5}{9^{\frac{5}{8}}}, 9^{\frac{1}{4}}\right)^{\frac{5}{8}}$. Write t	he answer as an inte	ger or a fraction in lo	owest terms.
	a. $\frac{81}{5}$ b. $-\frac{1}{3}$	$\frac{1}{81}$ c.	81	d. $\frac{1}{81}$
 10.	Simplify $\left(\frac{5}{2}a^{-2}b^{6}\right)^{-3}$. Write	the expression with J	positive exponents.	
	a. $\frac{125a^6}{8b^{18}}$ b. $\frac{3}{12}$	$\frac{3b^3}{25a^5}$ c.	125b ¹⁸ 8a ⁶	d. <u>8a6</u> 125b ¹⁸
 11.	Evaluate $(a^{-6}b^{-3})^3(a^5b^6)^2$ f a. 27 b2	for $a = -1$ and $b = 3$.	$\frac{1}{27}$	d. $-\frac{1}{27}$
 12.	Write $\sqrt{200}$ as a mixed radio a. $10\sqrt{2}$ b. 2.	cal. √50 c.	100 \sqrt{2}	d. 2√10
 13.	Expand. $(4x - 6)(2x - 5)$ a. $8x^2 - 32x + 30$ b. $8x^2 + 32x + 30$	c. d.	$8x^2 - 8x - 30$ $8x^2 + 8x - 30$	
 14.	Determine which trinomial is a. $x^2 - 5x + 6$ b. $x^2 + 2x + 6$	factorable. c. d.	$x^2 - 5x + 9$ $2x^2 + 5x + 6$	
 15.	Determine which trinomial ca a. $2x^2 - 9x - 5$ b. $3x^2 + x + 2$	nnot be factored. c. d.	$3x^2 + x - 2$ $2x^2 - 4x - 5$	
 16.	Factor the trinomial $x^2 + 7x + a$. $(x + 5)(x + 2)$ b. $(x - 5)(x - 2)$	10. c. d.	(x+5)(x-2) (x-5)(x+2)	
 17.	Factor the trinomial $2x^2 + 3x^2$ a. $(2x + 3)(x + 3)$ b. $(2x - 3)(x + 3)$	- 9. c. d.	(2x+3)(x-3) (2x-3)(x-3)	
 18.	Factor the trinomial $60x^2 - 27$ a. $(5x - 6)(12x + 9)$ b. $3(5x - 6)(4x + 3)$	/x − 54. c. d.	(5x - 6)(4x + 3) 3(5x + 6)(4x + 3)	
 19.	Factor the trinomial $-3x^2 - 6x^2$ a. $6(x-3)(x-4)$ b. $-4(x+6)(x-3)$	c. d.	-3(x+6)(x+4) -3(x-4)(x+6)	
 20.	Factor: $49b^2 - 64$ a. $(8b + 7)(8b - 7)$ b. $(7b + 8)(7b - 8)$	c. d.	(7b - 8)(7b - 8) (7b + 8)(7b + 8)	

21	. Factor: $4x^2 - 25y^2$		
	a. $(5x + 2y)(5x - 2y)$	c. $(2x + 5y)(2x - 5$	y)
	b. $(2x - 5y)(2x - 5y)$	d. $(2x+5)(2x-5)$	
22	Factor: $9m^2 - 42m + 49$		
	a. $(3m+7)^2$	c. (3 <i>m</i> − 49)(3 <i>m</i> −	1)
	b. $(3m-7)^2$	d. $(3m - 7)(3m +$	7)

- 23. Factor this polynomial expression: $2(3x-2)^2 + 9(3x-2) 5$ a. 2(3x-2)(x+5)c. 3(x+1)(6x-5)b. 2(3x+2)(x-5)d. 3(x-1)(6x+5)
 - 24. Factor: $0.5x^2 0.02$ a. 0.5(x+0.1)(x-0.1)c. 0.5(x+0.2)(x-0.2)b. (0.5x + 0.2)(x - 0.2)d. (0.5x + 0.1)(x - 0.1)

25. For a quadratic function, which characteristic of its graph is equivalent to the zero of the function? a. minimum point c. y-intercept d. x-intercept

- b. maximum point
- 26. Which graph represents the quadratic function $y = 2x + x^2$?





27. Which graph represents the quadratic function $y = x^2 + x - 1$?

28. What are the coordinates of the vertex of this graph of the quadratic function $y = x^2 - 2x + 2$? State whether it is a maximum point or a minimum point.



a. (1, 2); minimum pointb. (1, 2); maximum point

- c. (1, 1); maximum point
- d. (1, 1); minimum point

- 29. Identify the y-intercept of the graph of this quadratic function: $y = -3(x+3)^2 + 4$ a. 13 b. -23 c. -27 d. 23
- _____ 30. Which of the following describes the translation that would be applied to the graph of $y = x^2$ to get the graph of $y = x^2 + 5$?
 - a. Translate 5 units left c. Translate 5 units up
 - b. Translate 5 units down d. Translate 5 units right
 - _____ 31. Which statement is NOT true for the graph of $y = x^2 + q$?
 - a. When *q* is positive, the graph lies above the *x*-axis.
 - b. As q increases, the graph moves up.
 - c. The graph has the same size and shape as the graph of $y = x^2$.
 - d. When q is negative, the vertex is above the x-axis.
 - 32. Which statement is NOT true for the graph of $y = ax^2$?
 - a. The vertex of the graph is always at the origin.
 - b. When *a* is less than -1, the graph is the image of the graph of $y = x^2$ after a vertical stretch and a reflection in the *x*-axis.
 - c. When *a* is greater than 1, the graph is the image of the graph of $y = x^2$ after a vertical stretch.
 - d. When 0 < a < 1, the graph is the image of the graph of $y = x^2$ after a vertical compression and a reflection in the *x*-axis.

_ 33. Identify the coordinates of the vertex of the graph of this quadratic function: $y = \frac{1}{8}(x-4)^2 - 4$

a. (4,4) b. (-4,4) c. (-4,-4) d. (4,-4)



34. Match the quadratic function $y = 2x^2 + 2$ to a graph below.

_ 35. Determine an equation of this graph of a quadratic function.



36. Determine an equation of this graph of a quadratic function.





45. Identify the *x*-intercepts of the graph of this quadratic function: y = (x - 3)(x + 1)a. 3 and 1 b. 3 and -1 c. -3 and 1 d. -3 and -1

16	Determine the zeros of this and ductic function.	$y = x^2 - 4x - 32$	
 40.	a. $4 \text{ and } -8$ b. $-4 \text{ and } 8$	c. $4 \text{ and } 8$ d. $-4 \text{ and } -8$	
 47.	Determine the <i>x</i> -intercepts and the coordinates a. 2 and -4; (3, 1) b. 2 and 4; (3, 1)	s of the vertex of the graph of $y = x^2 - 6x + 8$. c. -2 and 4; $(-3, -1)$ d. -2 and -4 ; $(-3, 1)$	
 48.	Solve the following quadratic equation: $4x^2 - \frac{1}{2}$ a. $x = -\frac{1}{2}$ and $x = -\frac{3}{2}$ b. $x = \frac{1}{2}$ and $x = \frac{3}{2}$	$x^{-8x+3} = 0$ $x^{-8x+3} = 0$ $x = \frac{2}{3}$ and $x = 2$ x = -2 and $x = -6$	
 49.	Solve the following quadratic equation: $8x^2 - \frac{3}{8}$ and $x = 2$ b. $x = -\frac{3}{2}$ and $x = \frac{1}{2}$	-13x - 6 = 0 c. $x = \frac{3}{8}$ and $x = -2$ d. $x = \frac{1}{4}$ and $x = 3$	
 50.	Solve $(x+1)^2 = 43$.		
	a. $1 + \sqrt{43}$ and $1 - \sqrt{43}$ b. $-1 + \sqrt{43}$ and $-1 - \sqrt{43}$	c. $2\sqrt{11}$ d. $\sqrt{42}$	
 51.	Which radical expression simplifies to $2\sqrt{2}$? a. $\sqrt{4}$ b. $\sqrt{8}$	c. $\sqrt{16}$ d. $\sqrt{9}$	
 52.	Which radical expression simplifies to $9\sqrt{2}$? a. $\sqrt{32} - \sqrt{8} + 7\sqrt{2}$ b. $\sqrt{32} - 7\sqrt{2} + \sqrt{8}$	c. $\sqrt{32} + 7\sqrt{8} - \sqrt{2}$ d. $\sqrt{2} + 7\sqrt{8} - \sqrt{32}$	
 53.	Simplify by adding or subtracting like terms: 8 a. $6\sqrt{10}$ b. $\sqrt{78}$	$8\sqrt{13} - 7\sqrt{13} + 5\sqrt{13}$ c. $10\sqrt{13}$ d. $6\sqrt{13}$	
 54.	Simplify by adding or subtracting like terms: \sqrt{a} . $-8\sqrt{5}$ b. $-8\sqrt{3}$	$\sqrt{9} + \sqrt{125} - \sqrt{81} + \sqrt{3125}$ c. $30\sqrt{3} - 6$ d. $30\sqrt{5} - 6$	
 55.	Expand and simplify this expression: $-\sqrt{2} \left(\sqrt{2} \right)^2$ a. $-\sqrt{14} + 5\sqrt{2}$ b. $-7\sqrt{2} + \sqrt{10}$		
 56.	Expand and simplify this expression: $(\sqrt{7} + 7)^{2}$ a. $\sqrt{21} - 2\sqrt{7} + 7\sqrt{3} - 14$ b. $\sqrt{21} + 3\sqrt{7} + 7\sqrt{3} + \sqrt{49}$	$7 \Big) \Big(\sqrt{3} - 2 \Big)$ c. $7\sqrt{3} - 2\sqrt{7} + 7\sqrt{7} - 14$ d. $\sqrt{21} - 14\sqrt{7} - 14$	

____ 57. Rationalize the denominator: $\frac{7}{7\sqrt{5}}$

a.
$$\frac{7\sqrt{5}}{35}$$
 b. $\frac{7\sqrt{5}}{5}$ c. $\frac{35\sqrt{5}}{5}$ d. $\frac{49\sqrt{5}}{7}$

 $\begin{array}{c} \hline 58. & \text{Expand and simplify this expression: } \left(\sqrt{5} - 3\right) \left(5\sqrt{5} + 4\right) - \left(4\sqrt{5} - 5\right)^2 \\ a. & -92 + 29\sqrt{5} \\ b. & -18 + 31\sqrt{5} \end{array}$

 $59. Simplify this expression: \frac{-9\sqrt{5}-3}{\sqrt{5}}$ $a. \frac{-9-15\sqrt{5}}{5}$ $b. -225-3\sqrt{5}$ $c. \frac{-45\sqrt{5}-15}{5}$ $d. \frac{-45-3\sqrt{5}}{5}$ $c. \frac{-45-3\sqrt{5}}{5} \\
c. \frac{-45-3\sqrt{5}}{5} \\
c.$





____ 69. Simplify this expression: $\frac{5p}{2} \cdot \frac{4p}{p}$ b. $10p, p \neq -2$ c. $\frac{5p}{8}, p \neq 0$ a. $\frac{9p}{2}, p \neq 0$ d. $10p, p \neq 0$ $- \frac{70.}{\frac{2x+4}{x} \div \frac{2}{x-6}}$ a. $2x^2 - 8x - 24$. $x \neq 0$. $x \neq 6$ c. $\frac{(x+2)(x-6)}{x}$, $x \neq 0$, $x \neq 6$ b. $\frac{4(x+2)}{x(x-6)}$, $x \neq 0$, $x \neq 6$ d. $\frac{x-12}{x}$, $x \neq 0$, $x \neq 6$ ____ 71. Simplify. $\frac{5}{a} + \frac{9}{7}$ a. $\frac{14}{\alpha+7}$, $\alpha \neq -7$ c. $\frac{9a+35}{7a}$, $a \neq 0$ b. $\frac{9a+35}{a+7}$, $a \neq -7$ d. $\frac{14}{7\alpha}$, $\alpha \neq 0$ ____ 72. Simplify. $\frac{d+5}{d^2} + \frac{2}{d} - 3$ a. $\frac{d+4}{d^2}, d \neq 0$ c. $\frac{-3d^2 + 3d + 5}{d^2}, d \neq 0$ b. $\frac{-3d^2 + 3d + 5}{2d^2}, d \neq 0$ d. $\frac{d+4}{2d^2}$, $d \neq 0$ _____ 73. Simplify. $pq - \frac{p-q}{p} + \frac{p+q}{q}$ a. $1, p \neq 0, q \neq 0$ c. $\frac{p^2q^2 + p^2 + q^2 + 2pq}{p\alpha}, p \neq 0, q \neq 0$ b. $\frac{p^2q^2 + p^2 + q^2}{pq}$, $p \neq 0, q \neq 0$ d. $\frac{pq}{p+q}$, $p \neq 0$, $q \neq 0$ _____ 74. Simplify. $\frac{r+6}{r-2} + \frac{4}{2-r}$ a. $\frac{r+10}{r-2}, r \neq 2$ c. $\frac{r+10}{(r-2)^2}$, $r \neq 2$ d. $\frac{r+2}{r-2}, r \neq 2$ b. $\frac{r+2}{(r-2)^2}, r \neq 2$

$$---- 75. \quad \text{Simplify.} \\ \frac{x-2}{x+6} + \frac{x+4}{x-1} \\ a. \quad \frac{2x^2 + 7x + 26}{x+5}, \ x \neq -6, \ x \neq 1, \ x \neq -5 \\ b. \quad \frac{x+2}{x+5}, \ x \neq -6, \ x \neq 1, \ x \neq -5 \\ c. \quad \frac{2x^2 + 7x + 26}{(x+6)(x-1)}, \ x \neq -6, \ x \neq 1 \\ d. \quad \frac{x+2}{(x+6)(x-1)}, \ x \neq -6, \ x \neq 1 \\ \end{array}$$

Simplify.

$$\frac{a}{a^2 - 144} - \frac{3a - 1}{a^2 + 10a - 24}$$
a.

$$\frac{-2a^2 + 35a - 12}{(a + 12)(a - 12)(a - 2)}, a \neq 12, a \neq -12, a \neq 2$$
b.

$$\frac{3a^2 - a}{-10a - 120}, a \neq 120$$
c.

$$\frac{-2a + 1}{-10(a + 12)}, a \neq -12$$
d.

$$\frac{-2a + 1}{(a + 12)(a - 12)(a - 2)}, a \neq 12, a \neq -12, a \neq 2$$

$$\frac{16}{n} = \frac{n}{9}$$
a. $n = \frac{9}{16}$
b. $n = 12 \text{ or } n = -12$
c. $n = 144 \text{ or } n = -144$
d. $n = \frac{16}{9}$

____ 78. Solve. $\frac{w-5}{w^2} = \frac{1}{20}$ a. w = 10b. w = 10 or w = -10

c. w = -5d. no solution

---- 79. Simplify:
$$\frac{\frac{3}{4} + 2x}{\frac{3}{4} - 2x}$$

a. $\frac{3 - 16x}{3 + 8x}$
b. -1
c. $-\frac{3}{16x}$
d. $\frac{3 + 8x}{3 - 8x}$

80. Solve

$\frac{25}{2} = \frac{w-6}{2}$		
w-б w		
a. $w = 1$ or w	= -36	
b. $w = -1$ or w	v = 36	

81. A freight train travels 60 km. A single locomotive pulls the train for the first half of the trip, then a second locomotive is added, doubling the speed of the train. If the total time for the trip is 54 min, what is the speed of the train with one locomotive? d. 50 km/h

c. w = 1 or w = 36d. no solution

- b. 133 km/h c. 233 km/h a. 267 km/h
- 82. The graph of -4x + 7y > 1 is



- ____ 84. Which interval below is the solution of the inequality $4 + \frac{3}{4}x < 10$?
 - a. x < 8 b. x > 8 c. x < -8 d. x > -8
- $\begin{array}{c} \hline 85. & \text{Which interval below is the solution of the inequality } 3 + x \le 6? \\ a. & [3, \infty) & b. & [-\infty, -3) & c. & (-\infty, 2] \\ \end{array}$

86. Solve the linear inequality 13x - 11 < 13 + 14x. Write the solution in interval notation. a. x > -24; $(-24, \infty)$ b. x < -3; $(-\infty, -3)$ c. x > 8; $(8, \infty)$ d. x < -24; $(-\infty, -24)$

87. Which graph represents the solution to the inequality $y \le -5(x+3)^2 + 4$?



88. Which point does *not* satisfy the inequality $y > -2(x-3)^2 + 8$?

a.	(-9, -234)	с.	(5,16)
b.	(1,1)	d.	(2,0)

89. Solve the quadratic inequality: $x^2 - 2x \ge 3$

a.
$$-3 \le x \le 1$$
 c. $x \le 3 \text{ or } x \ge 1$

 b. $x \le -1 \text{ or } x \ge 3$
 d. $-3 \le x \le -1$

____ 90. The solution set to the inequality $-3x^2 \le -9x + 6$ is

a.
$$\{x \mid 1 \le x \le 2, x \in R\}$$

b. $\{x \mid -2 \le x \le -1, x \in R\}$
c. $\{x \mid x \le -2 \text{ or } x \ge -1, x \in R\}$
d. $\{x \mid x \le 1 \text{ or } x \ge 2, x \in R\}$

91. Which interval below is the solution of the inequality $x^2 - x - 90 > 0$? a. $(-\infty, -9)$ or $(10, \infty)$ b. [9, 10]c. $(-\infty, -10]$ or $[9, \infty)$ d. (-9, 10]

92. Solve the quadratic inequality $5x^2 + 14x - 3 \ge 0$ algebraically. Write the solution in interval notation. Show the solution on a number line. a. $x \le -3$ or $x \ge 0.2$: $(-\infty, -3)$ or $(0.2, \infty)$

$$\begin{array}{c} \begin{array}{c} 0.2 \\ \hline & -7 & -6 & -5 & -4 & -3 & -2 & -1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \end{array}$$

$$\begin{array}{c} 0.2 \\ \hline & -7 & -6 & -5 & -4 & -3 & -2 & -1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \end{array}$$

$$\begin{array}{c} 0.2 \\ \hline & -7 & -6 & -5 & -4 & -3 & -2 & -1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \end{array}$$

$$\begin{array}{c} 0.2 \\ \hline & -7 & -6 & -5 & -4 & -3 & -2 & -1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \end{array}$$

$$\begin{array}{c} 0.2 \\ \hline & -7 & -6 & -5 & -4 & -3 & -2 & -1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \end{array}$$

$$\begin{array}{c} 0.2 \\ \hline & -7 & -6 & -5 & -4 & -3 & -2 & -1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \end{array}$$

$$\begin{array}{c} 0.2 \\ \hline & -8 & -7 & -6 & -5 & -4 & -3 & -2 & -1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 \end{array}$$

$$\begin{array}{c} 0.2 \\ \hline & -8 & -7 & -6 & -5 & -4 & -3 & -2 & -1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 \end{array}$$

$$\begin{array}{c} 0.2 \\ \hline & -8 & -7 & -6 & -5 & -4 & -3 & -2 & -1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 \end{array}$$

93. Point P(7, 9) is on the terminal arm of an angle θ in standard position. Determine the measure of θ to the nearest degree.
 a. θ = 63°
 b. θ = 38°
 c. θ = 52°
 d. θ = 33°

4 5 6

- 94. An angle θ has its terminal arm in Quadrant 2. Which primary trigonometric ratio is greater than 0? a. $\cos \theta$ b. $\tan \theta$ c. $\sin \theta$ d. all 3 ratios
- ____ 95. Determine the reference angle for the angle 290° in standard position. a. 110° b. 20° c. 290° d. 70°

-8 -7 -6 -5 -4 -3 -2 -1 0 1 2 3

- $_{-}$ 96. What are the three other angles in standard position that have a reference angle of 54°?
 - a. 99°, 144°, 234°
 - b. 108°, 162°, 216° d. 126°, 234°, 306°
- ____ 97. The coordinates of a point P on the terminal arm of an angle are shown. What are the exact trigonometric ratios for $\sin \theta$, $\cos \theta$, and $\tan \theta$?

c. 144°, 234°, 324°



98. Which angle is NOT coterminal with an angle of 190° in standard position? a. -170° b. -530° c. 370° d. 550°

99. Which expression represents the measures of all the angles coterminal with an angle of 203° in standard position?

a.	$23^\circ + k360^\circ, k \in I$	с.	$203^{\circ} + k180^{\circ}, k \in I$
b.	$203^{\circ} + k360^{\circ}, k \in R$	d.	$203^{\circ} + k360^{\circ}, k \in I$

_____100. For ΔDEF , write the Sine Law equation you would use to determine the measure of $\angle E$.



101. For $\triangle ABC$, determine the measure of $\angle A$ to the nearest degree.



102. For ΔXYZ , determine the measure of $\angle Z$ to the nearest degree and the measure of XZ to the nearest tenth of a centimetre.



a.	$\angle Z = 28^\circ; XZ = 7.3 \text{ cm}$	с.	$\angle Z = 53^\circ; XZ = 8.0 \text{ cm}$
b.	$\angle Z = 59^\circ; XZ = 4.8 \text{ cm}$	d.	$\angle Z = 30^{\circ}; XZ = 12.1 \text{ cm}$

____ 103. For △PQR, write the Cosine Law equation you would use to determine the measure of $\angle Q$.









105. In △ABC, AB = 6 cm, BC = 8.5 cm, and AC = 5.8 cm. Determine the measure of ∠B to the nearest degree.

